



# Addition Strategies



addend     addend     sum  
 $8 + 7 = 15$

<b>Count On</b>	Start with the larger number and count up. <i>Use when adding 1, 2, or 3.</i>	$+1 +2 +3$
<b>Making Ten</b> <i>Ten Partners</i>	There are number pairs that make 10. $10+0 \quad 9+1 \quad 8+2 \quad 7+3 \quad 6+4 \quad 5+5$	
<b>Doubles</b> <i>+1 and +2</i> <i>Near Doubles</i>	Adding a number to itself makes a double. $5 + 5 = 10$ Double the number and add one or two more. <i>If you know <math>5+5=10</math>, then <math>5+7</math> is two more, or 12</i>	
<b>Plus 10</b>	When 10 is added to a number, the tens-place digit increases by one. $23 + 10 = 33$	
<b>Plus 9</b> <i>See 9. Make 10.</i>	Decompose the other addend to add one to the 9. <i>("Need one more, look next door")</i> $15 + 9. \text{ Think } 14 + 10$	
<b>Plus 8</b> <i>See 8. Make 10.</i>	Decompose the other addend to add two to the 8. <i>("Need two more, look next door")</i> $14 + 8. \text{ Think } 12 + 10$	
<b>Add in Small Steps</b>	Decompose the smaller number into parts so that you can add up to create a 10. $28 + 6 = 28 + (2 + 4) = 30 + 4 = 34$	
<b>Commutative Property</b> <i>Turn Arouds</i>	Order doesn't matter when adding. $8 + 3 = 11 \quad 3 + 8 = 11$	
<b>Traditional Algorithm</b>	Stack the numbers lining up the digits according to place value. Add the 1s first, regroup if needed, continue with the 10s and so on.	$\begin{array}{r} 1 \\ 35 \\ +56 \\ \hline 91 \end{array}$



# Subtraction Strategies



minuend    subtrahend    difference

$9 - 7 = 2$

<b>Count Back</b>	Start with the larger number and count back. Use when subtracting 1, 2, or 3	$-1 - 2 - 3$
<b>Count Up</b>	Count the steps from the subtrahend to the minuend to get the difference.	$21 - 18 =$ 
<b>Think Addition</b>	To subtract, think of the related addition fact.	$15 - 8 = \boxed{?}$ think $8 + \boxed{?} = 15$
<b>Ten Partners</b>	If you know the addition Ten Partners, then you know the related subtraction facts.	$7 + 3 = 10$ so $10 - 3 = 7$
<b>Half</b>	If you know the double fact then you know the related subtraction fact.	$6 + 6 = 12$ so $12 - 6 = 6$
<b>Minus 10</b>	When 10 is subtracted from a number, the tens-place digit decreases by one.	$23 - 10 = 13$
<b>Minus 9</b>	Think of the number as a 10 and then add one. See 9. Think 10.	$15 - 9$ . Think $15 - 10 + 1$
<b>Minus 8</b>	Think of the number as a 10 and then add two. See 8. Think 10.	$27 - 8$ . Think $27 - 10 + 2$
<b>Subtract in Small Steps</b>	Decompose the subtrahend into smaller parts so that you can subtract to a 10 or a multiple of 10.	$24 - 7$ . Think splitting 7 into 4 and 3 first. Then $24 - 4 = 20$ then $20 - 3 = 17$
<b>Constant Difference</b>	Add or subtract the same amount to both the minuend and the subtrahend to make the problem easier to solve. Compensation	$43 - 25 = 43 (+5) - 25 (+5) = 48 - 30$
<b>Traditional Algorithm</b>	Stack the numbers lining up the digits according to place value. Subtract the 1s first, regroup if needed, continue with the 10s and so on.	

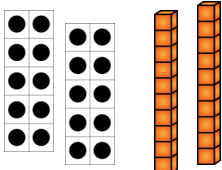



# Multiplication Strategies



factor      factor      product

$8 \times 4 = 32$

FOUNDATIONAL FACTS	<b>Twos</b>	Multiplying by 2 is doubling the number. Doubles	$2 \times 7$ . Think double 7. Think $7 + 7$
	<b>Tens</b>	Multiplying by 10 increases a number tenfold. Think ten-frames and base ten blocks.	$10 \times 2 = 20$ 
	<b>Fives</b>	Think <b>skip counting</b> by 5's or think half of multiplying by 10.	$5 \times 2 = 10$
	<b>Ones</b>	Multiplying by 1 equals the number because it is 1 group.	$6 \times 1 = 6$ 
	<b>Zeros</b>	If you multiply a number by 0 the product is always 0.	$9 \times 0 = 0$
BUILDING ON THE FOUNDATION	<b>Threes</b>	Multiplying by 3 can be thought of as doubling the number and then adding 1 more group, or as tripling the number.	$4 \times 3$ . Think $4 \times 2$ and add one more group of 4.
	<b>Fours</b>	Double the number, and then double it again. Double Double	$4 \times 7$ . Think $(2 \times 7) + (2 \times 7)$
	<b>Sixes</b>	Multiplying by 6 can be thought of as doubling a multiple of 3.	$6 \times 7$ . Think $(3 \times 7) + (3 \times 7)$
	<b>Nines</b>	Think of the 9 as a 10, then subtract one group. See 9. Think 10.	$8 \times 9$ . Think $8 \times 10 - 8$
	<b>Eights</b>	Multiplying by 8 is double multiplying by 4. Double Double Double	$7 \times 8$ . Think $(7 \times 2) + (7 \times 2) + (7 \times 2) + (7 \times 2)$ or $(7 \times 4) + (7 \times 4)$
<b>Sevens</b>	Decompose the 7 and multiply in smaller steps (Distributive Property) Multiplying Small Steps	$4 \times 7$ . Think $(4 \times 2) + (4 \times 5)$	
<b>Commutative Property</b>	Order doesn't matter when multiplying.	$4 \times 6 = 24$ and $6 \times 4 = 24$	



# Division Strategies



dividend    divisor    quotient

$$8 \div 4 = 2$$

<b>Division by 0</b>	0 divided by any number is 0. If there are no groups there is nothing to divide. $0 \div 9 = 0$
<b>A Number Divided by Itself</b>	A number divided by itself is 1. $5 \div 5 = 1$ $65 \div 65 = 1$
<b>Division by 1</b>	A dividend divided by 1 equals the number. $9 \div 1 = 9$ $204 \div 1 = 204$
<b>Half</b> <i>Divided by 2</i>	A dividend divided by 2 is half. Use double facts to solve. $8 \div 2 = 4$
<b>Think Multiplication</b>	Use multiplication to solve division problems. $27 \div 9 = $ <input type="text" value="3"/> <b>Think</b> $9 \times $ <input type="text" value="3"/> $ = 27$
<b>Half and Double</b>	Halve the dividend, double the quotient. $64 \div 4$ . Think half of 64 is 32, So $32 \div 4 = 8$ . Then double the quotient (8). $8 \times 2 = 16$ .
<b>Divide in Small Steps</b> <i>Factor the Divisor</i>	Decompose the divisor into smaller parts (factors) so that you can make the problem easier to solve. $54 \div 18$ . Think $54 \div 6 \div 3 = 9 \div 3 = 3$
<b>Compensation</b>	Multiply or divide the dividend and the divisor by the same number to make the problem easier to solve. $48 \div 12 = (48 \div 4) \div (12 \div 4) = 12 \div 3$
<b>Cancel Zeros</b> <i>Dividing by a Multiple of 10 First</i>	Remove the same number of zeroes from the end of both the dividend and the divisor. $360 \div 60$ . Think $36 \div 6$